

# Rates and transition paths from force spectroscopy experiments

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**MAX PLANCK**  
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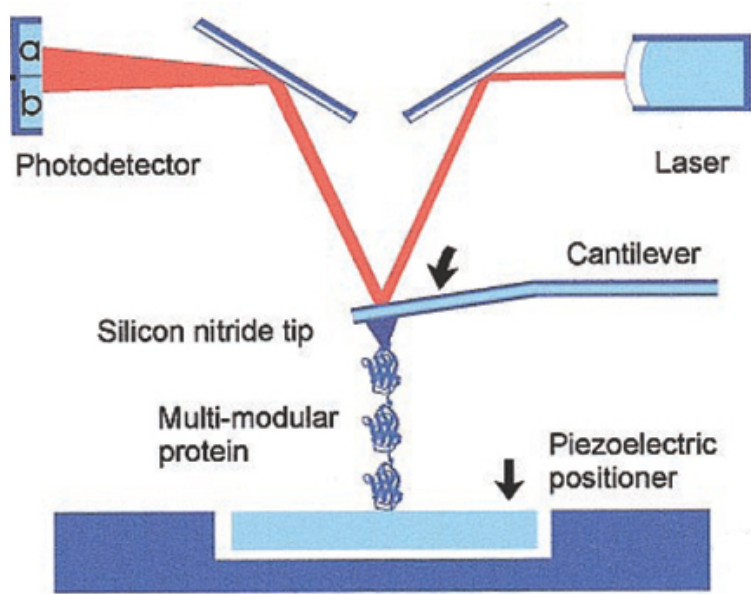


# Outline

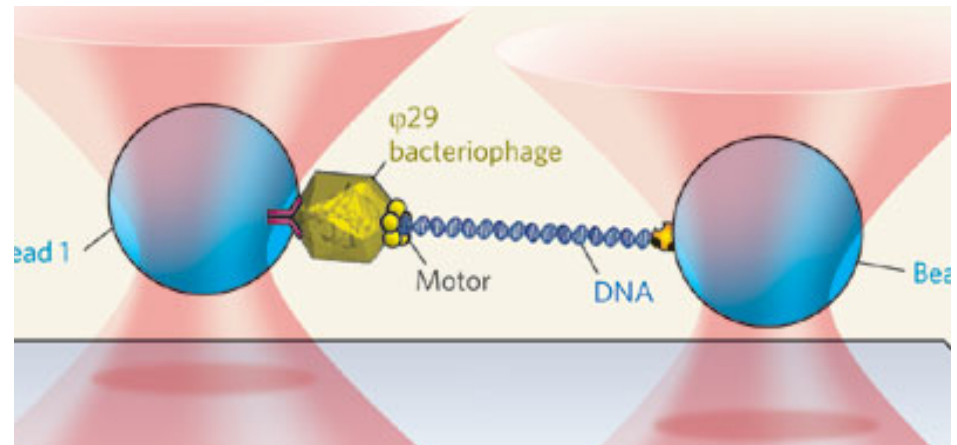
- \* Atomic force spectroscopy
- \* Extracting information from the experiments
- \* Artifacts of the apparatus
- \* Conclusions

# Motivation

# Single-molecule force spectroscopy



Atomic Force Microscopy (AFM)



Optical Tweezers

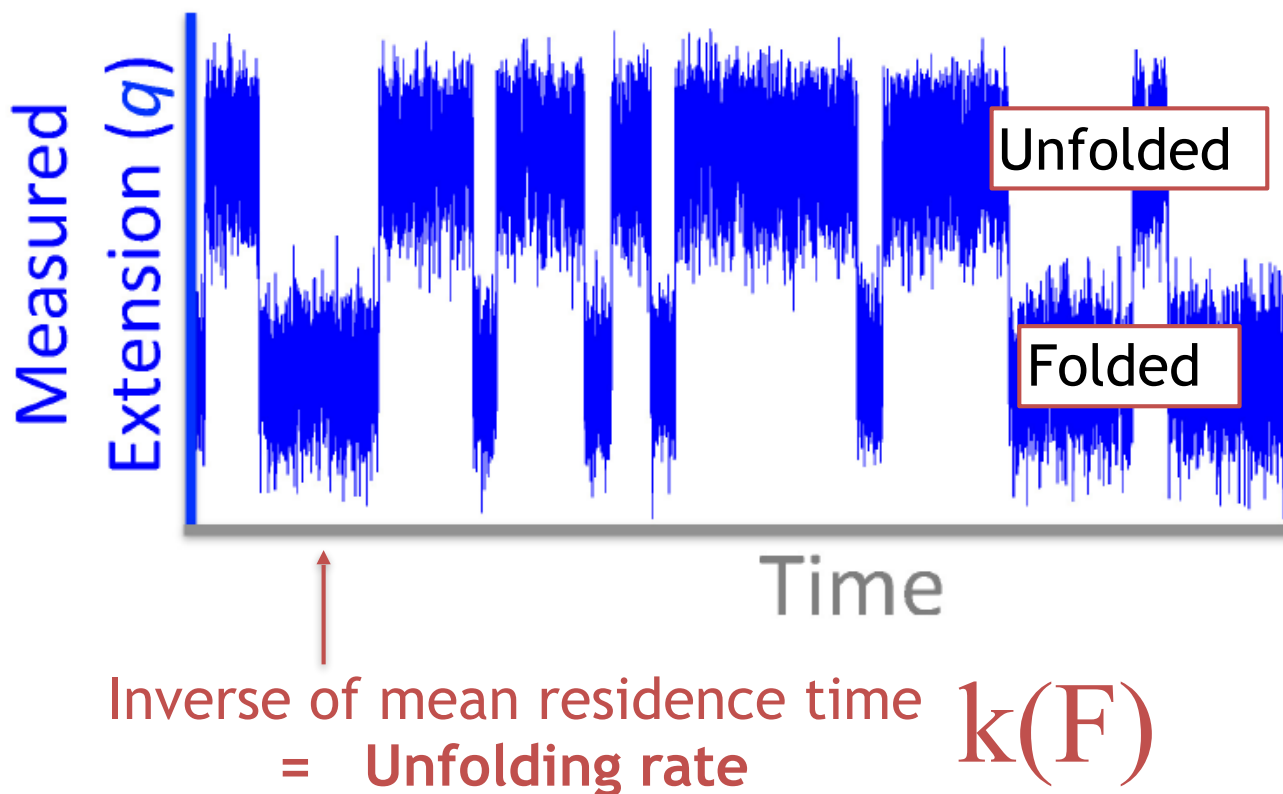
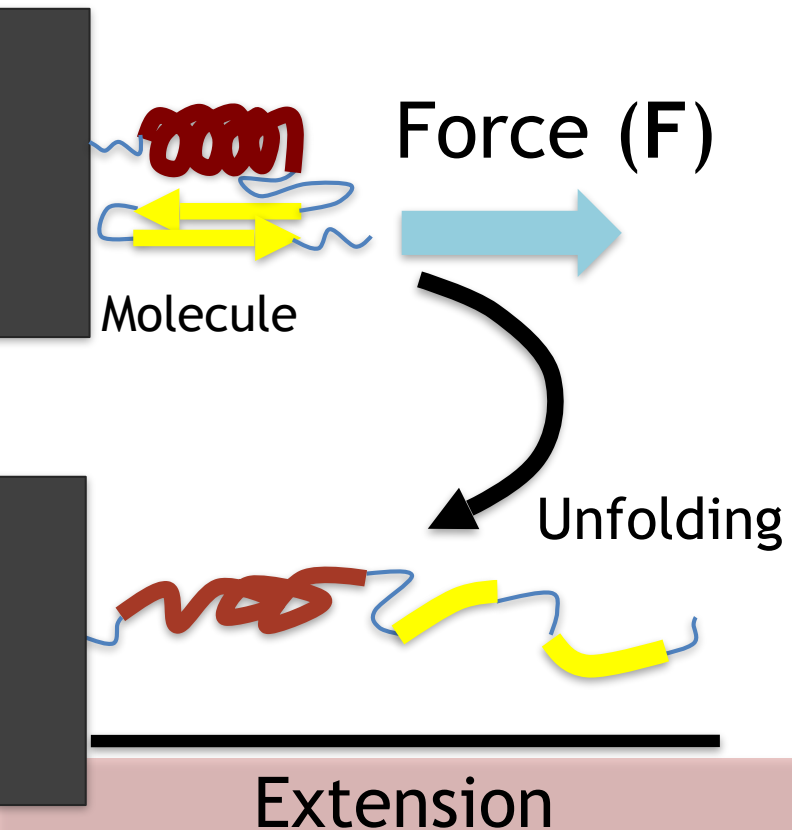
# Single-molecule



Dr. Gerhard Hummer

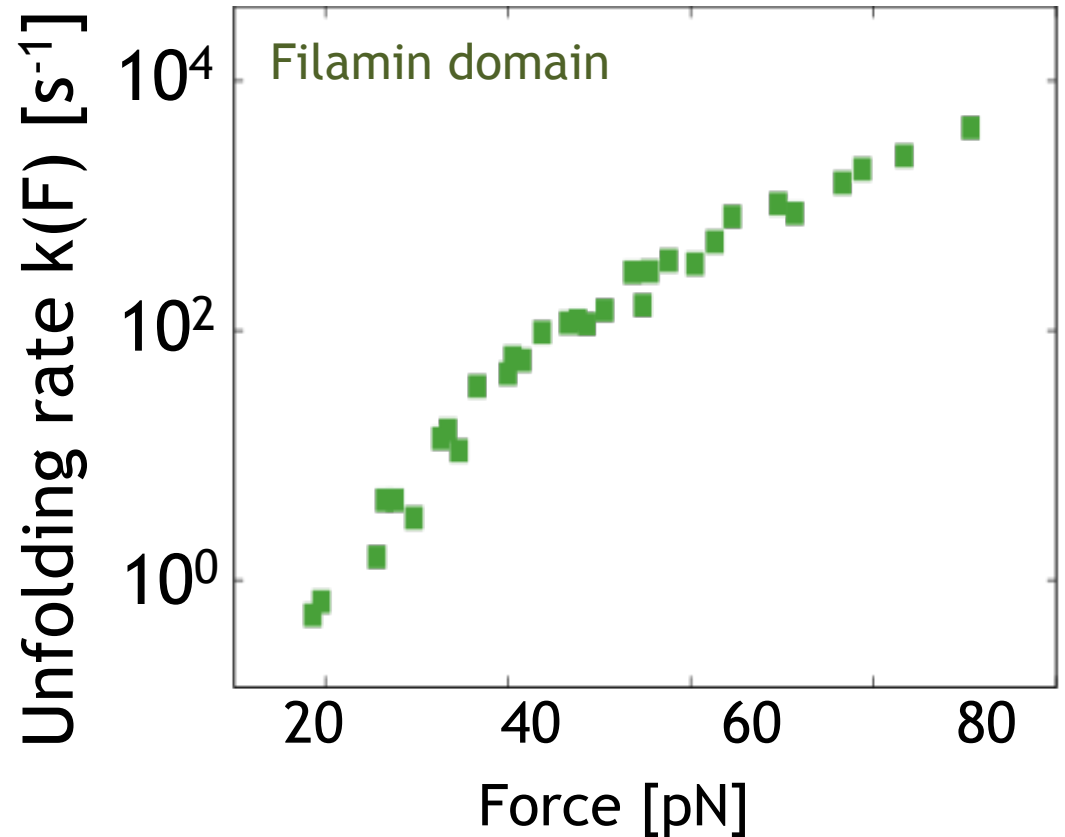
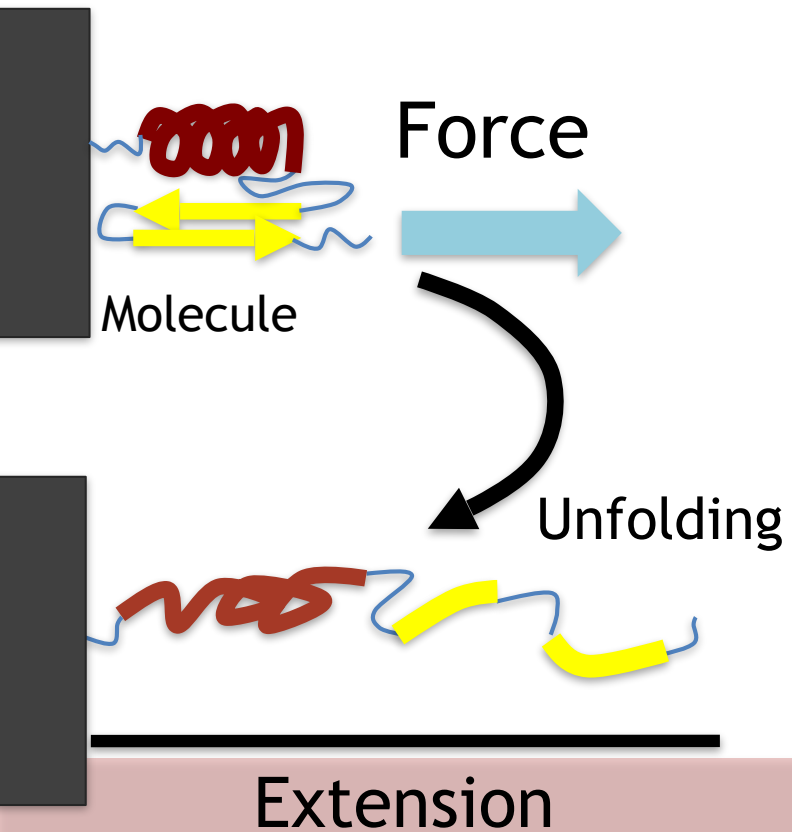


Dr. Attila Szabo



# Single-molecule

Force-dependent unfolding rate  $k(F)$  as a function of force:

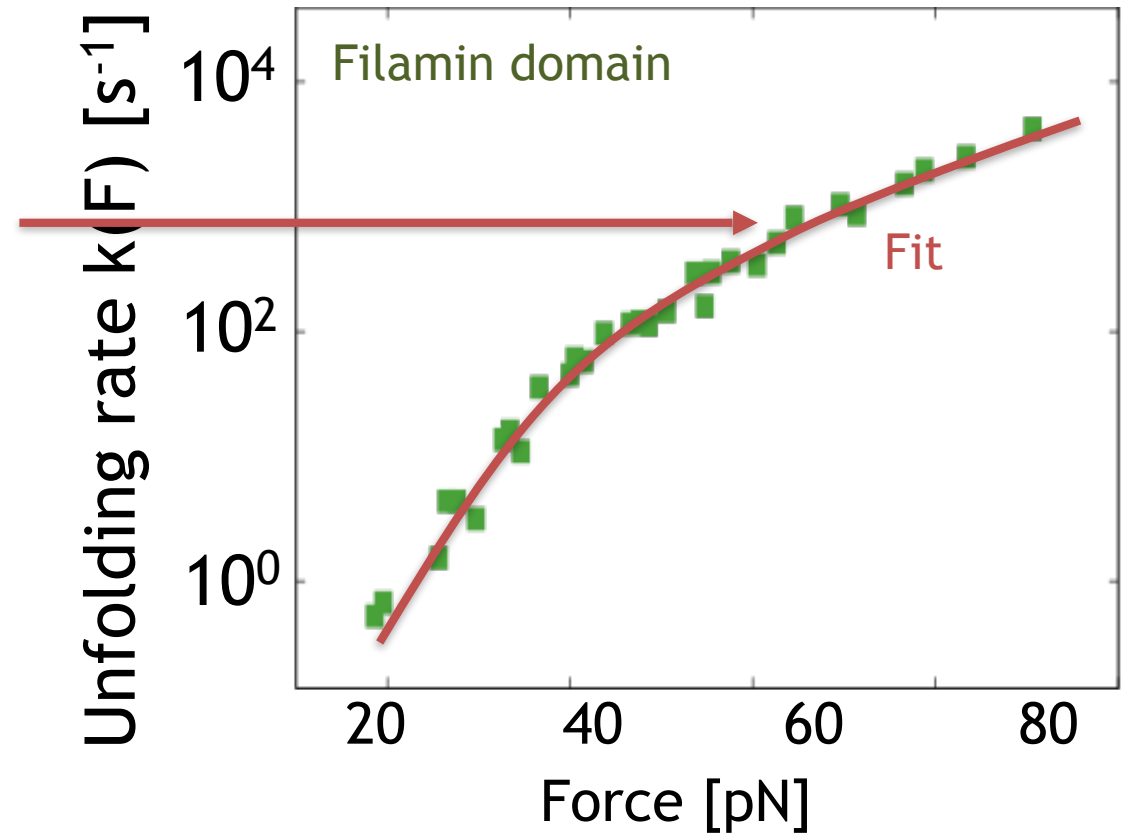
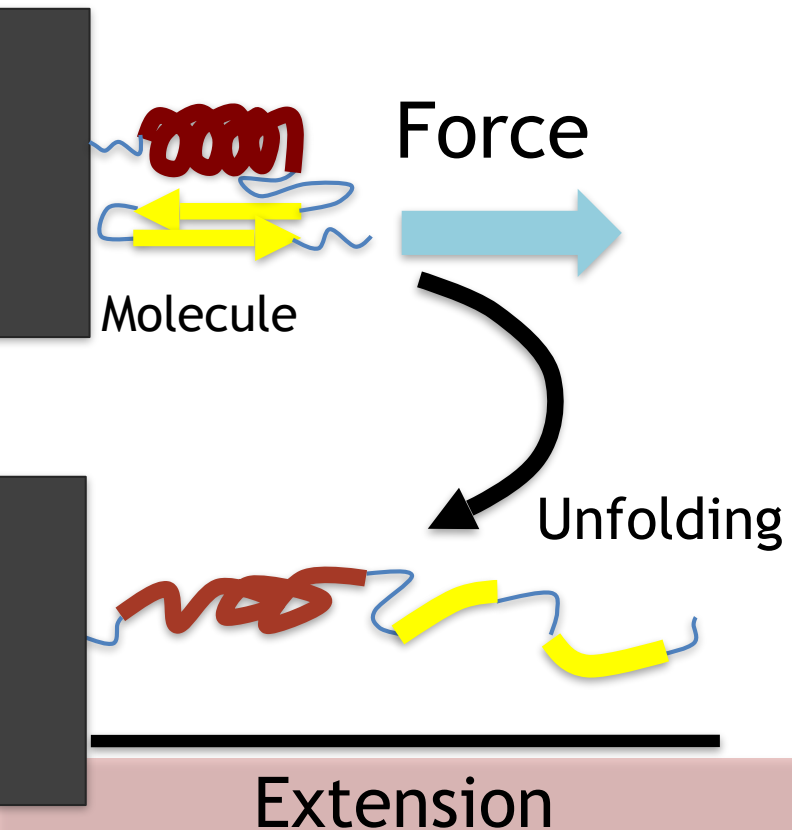


What can we learn from the data? **Information at  $F=0$ ?**

# Extracting information from the experimental traces

# Single-molecule

Force-dependent unfolding rate  $k(F)$  as a function of force:

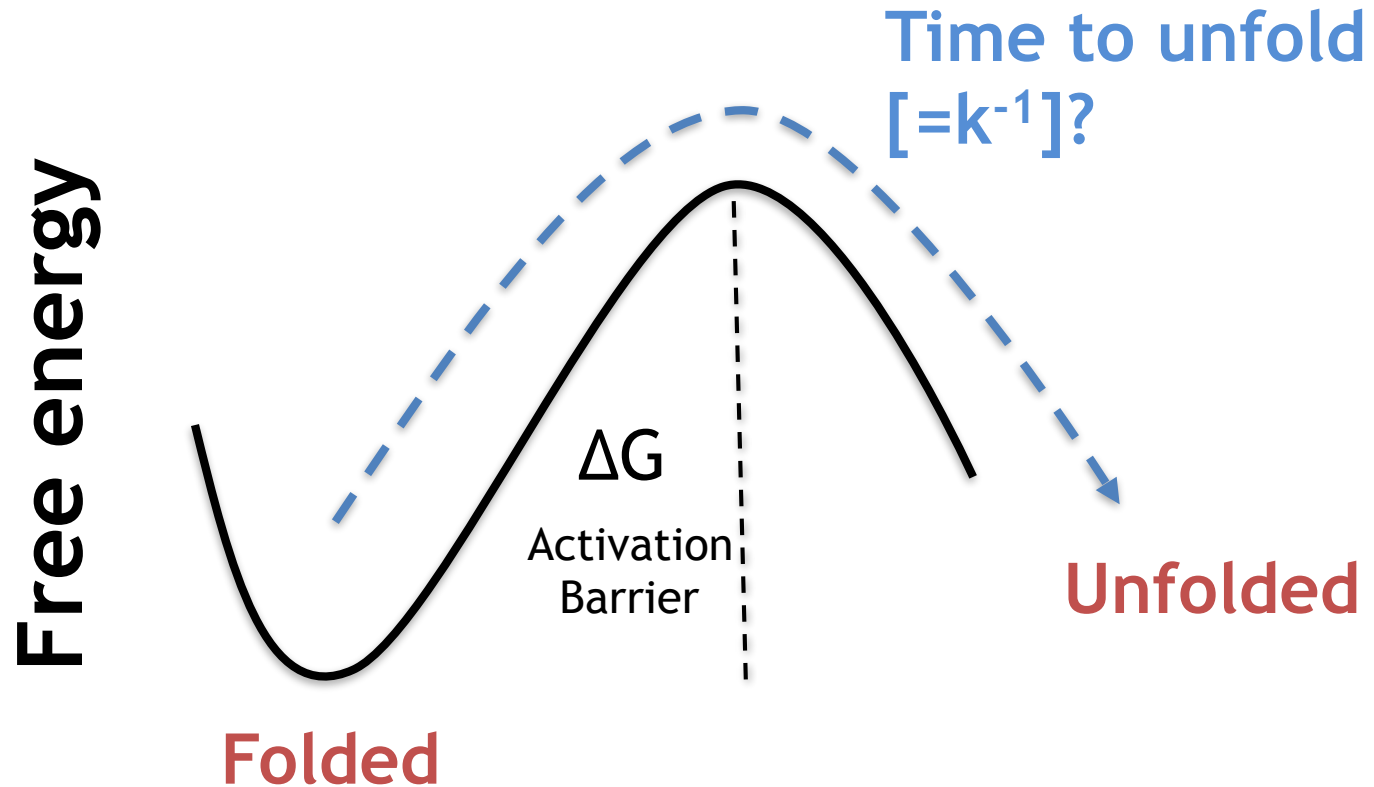


What can we learn from the data? **Information at  $F=0$ ?**



The unfolding process is modelled  
in 1D using **Kramers Theory**:  
Single-well potential

Single-  
molecule

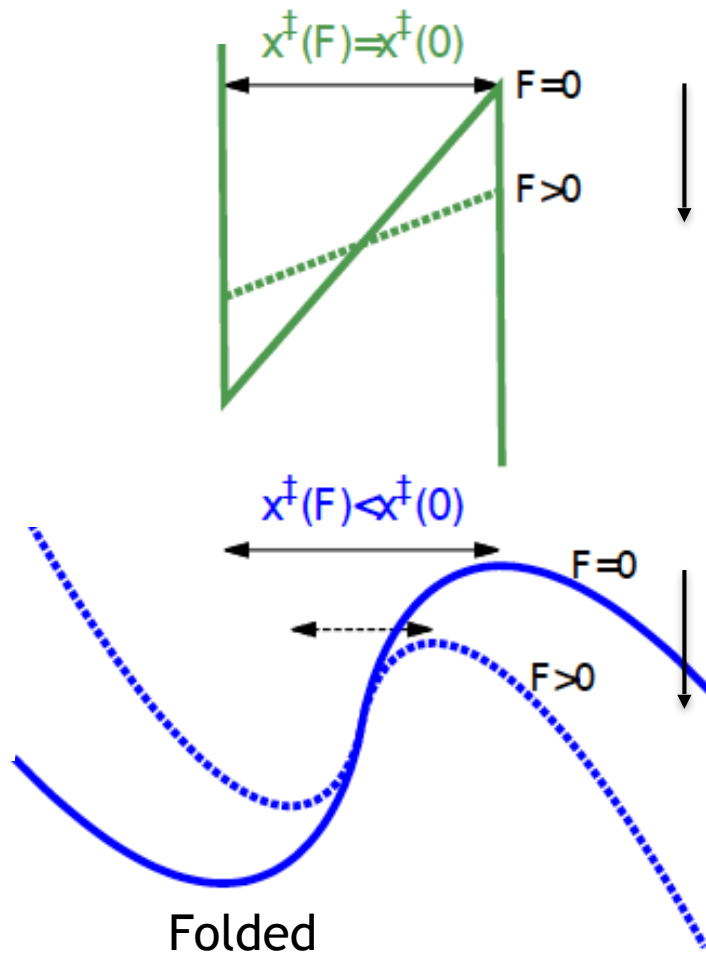


$$k_0^{-1} = \frac{1}{D} \int_{\ddagger} e^{\beta G(x)} dx \int_{\text{well}} e^{-\beta G(x)} dx$$

# Effect of force on a general class of 1D free energy surfaces:

Single-molecule

$$G(x) = G_0(x) - Fx$$



Force lowers the activation barrier

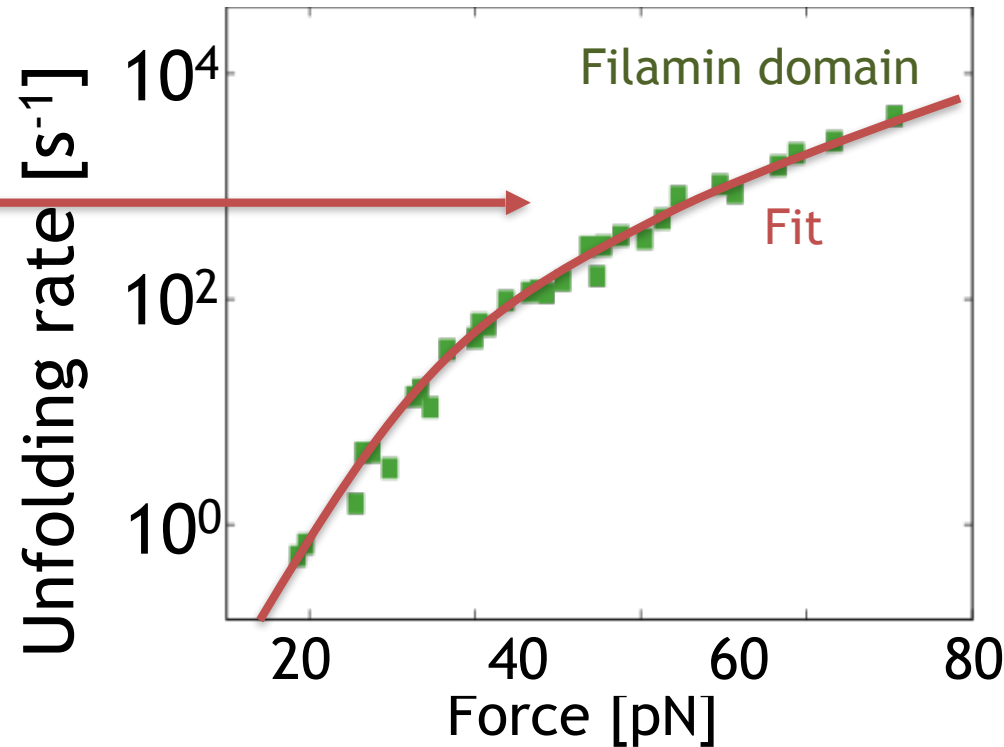
Energy surfaces that allows us to calculate  $k(F)$ , and the probability distribution of rupture forces  $p(F)$  analytically

# Single-molecule

## Kramers theory over free Energy surfaces:

Analytical expression of unfolding rate

$$k(F) = k_0 \left(1 - \frac{\mu F x^\ddagger}{\Delta G^\ddagger}\right)^{2 - \frac{1}{\mu}} e^{-\beta \Delta G^\ddagger} \left[1 - \left(1 - \frac{\mu F x^\ddagger}{\Delta G^\ddagger}\right)^{1/\mu}\right]$$



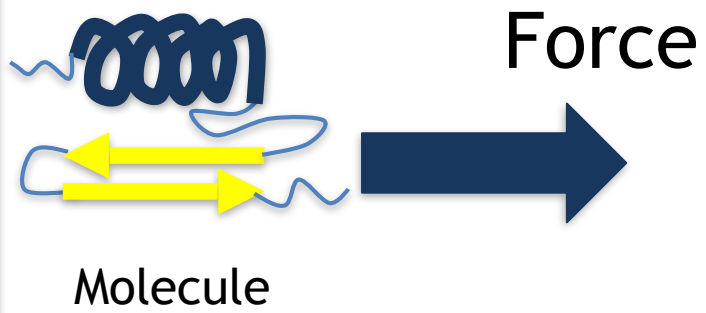
Extract information of the intrinsic (F=0) free energy and dynamics

# Artifacts of the apparatus

However, there are debates in the field of atomic force spectroscopy...

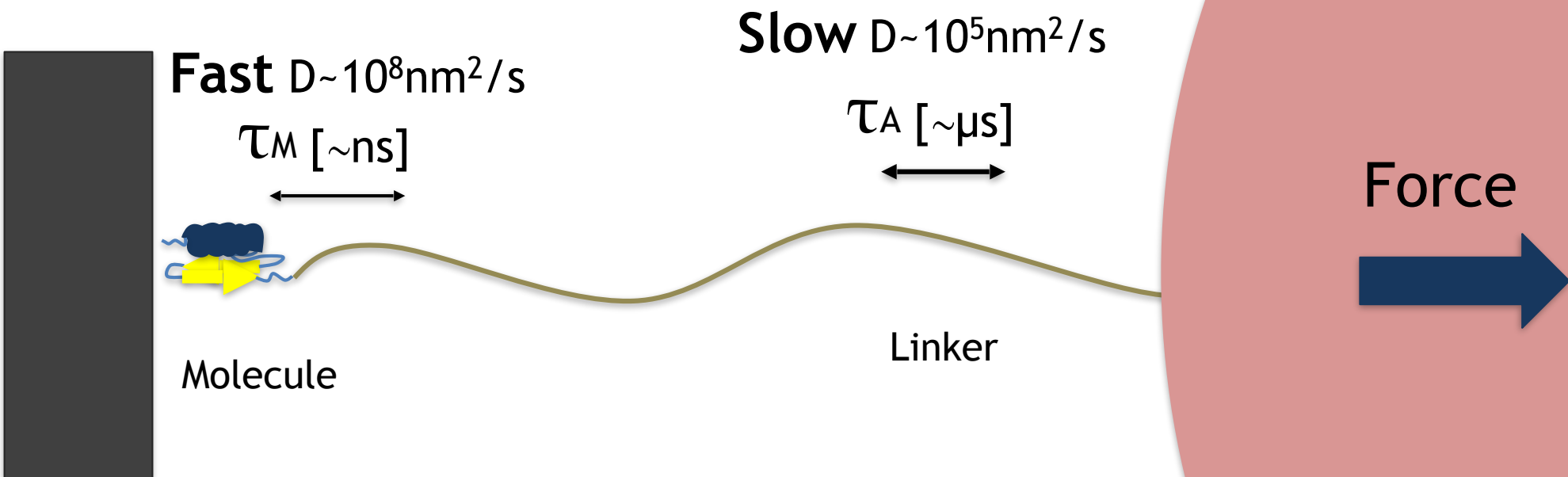
Single-  
molecule

Ideal case:



Single-  
molecule

In reality:



What about the huge apparatus?

# Single-molecule

What are the artifacts of the apparatus on the measured rate of unfolding?

## Effects of apparatus:

Hyeon C, Thirumalai D (2008) Multiple probes are required to explore and control the rugged energy landscape of RNA hairpins. *J. Am. Chem. Soc.* 130(5):1538–1539.

Hyeon C, Morrison G, Thirumalai D (2008) Force-dependent hopping rates of RNA hairpins can be estimated from accurate measurement of the folding landscapes. *Proc. Natl. Acad. Sci. U.S.A.* 105(28):9604–9609.

Hyeon C, Morrison G, Pincus DL, Thirumalai D (2009) Refolding dynamics of stretched biopolymers upon force quench. *Proc. Natl. Acad. Sci. U.S.A.* 106(48):20288–20293.

West DK, Paci E, Olmsted PD (2006) Internal protein dynamics shifts the distance to the mechanical transition state. *Phys. Rev. E* 74(6):061912.

Dudko OK, Hummer G, Szabo A (2008) Theory analysis and interpretation of single-molecule force spectroscopy experiments. *Proc. Natl. Acad. Sci. U.S.A.* 105(41):15755–15760.

Hummer G, Szabo A (2010) Free energy profiles from single-molecule pulling experiments. *Proc. Natl. Acad. Sci. U.S.A.* 107(50):21441–21446.

Maitra A, Arya G (2010) Model Accounting for the Effects of Pulling-Device Stiffness in the Analyses of Single-Molecule Force Measurements. *Phys. Rev. Lett.* 104(10):108301.

Maitra A, Arya G (2011) Influence of pulling handles and device stiffness in single-molecule force spectroscopy. *Phys. Chem. Chem. Phys.* 13(5):1836–1842.

Berkovich R, Garcia-Manyes S, Urbakh M, Klafter J, Fernandez JM (2010) Collapse Dynamics of Single Proteins Extended by Force. *Biophys. J.* 98(11):2692–2701.

Berkovich R, Garcia-Manyes S, Klafter J, Urbakh M, Fernandez JM (2010) Hopping around an entropic barrier created by force. *Biochem. Biophys. Res. Commun.* 403(1):133–137.

Hinczewski M, von Hansen Y, Netz RR (2010) Deconvolution of dynamic mechanical networks. *Proc. Natl. Acad. Sci. U.S.A.* 107(50):21493–21498.

Dudko OK, Graham TGW, Best RB (2011) Locating the Barrier for Folding of Single Molecules under an External Force. *Phys. Rev. Lett.* 107(20):208301.

Friddle RW, Noy A, De Yoreo JJ (2012) Interpreting the widespread nonlinear force spectra of intermolecular bonds. *Proc. Natl. Acad. Sci. U.S.A.* 109(34):13573–13578.

Berkovich R et al. (2012) Rate limit of protein elastic response is tether dependent. *Proc. Natl. Acad. Sci. U.S.A.* 109(36):14416–14421.

The conclusions vary from one extreme where the **effect is negligible**, to the other, where the observed **rates have little to do with the dynamics** of the molecule of interest.

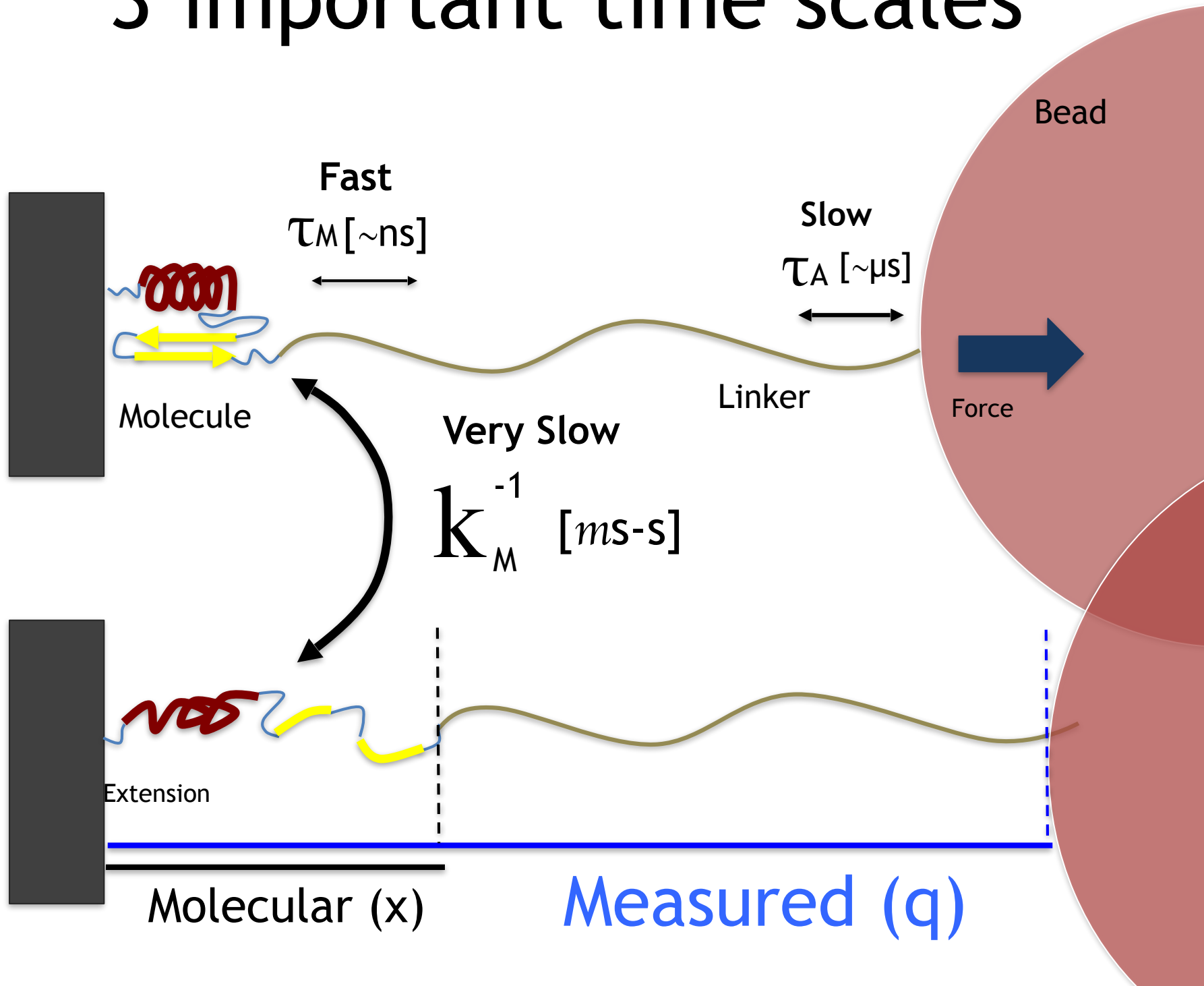
(and many more...)



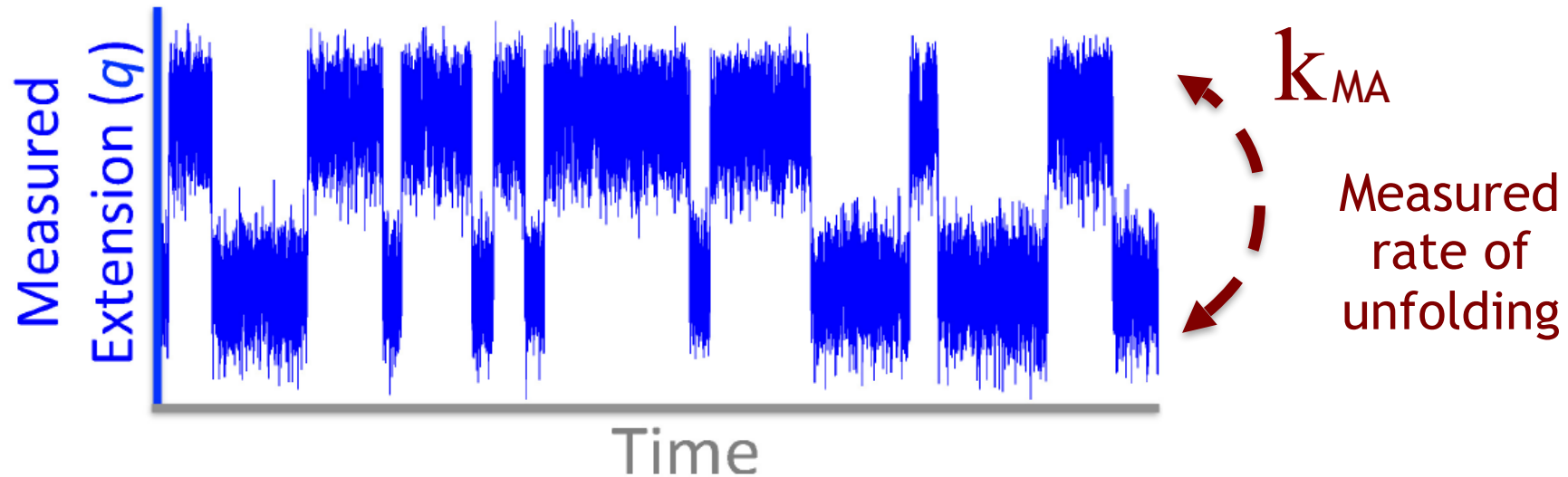
## Single- molecule

How does the measured rate compare to the molecular rate (in the ideal case that force could be applied directly to the molecule)?

# 3 important time scales

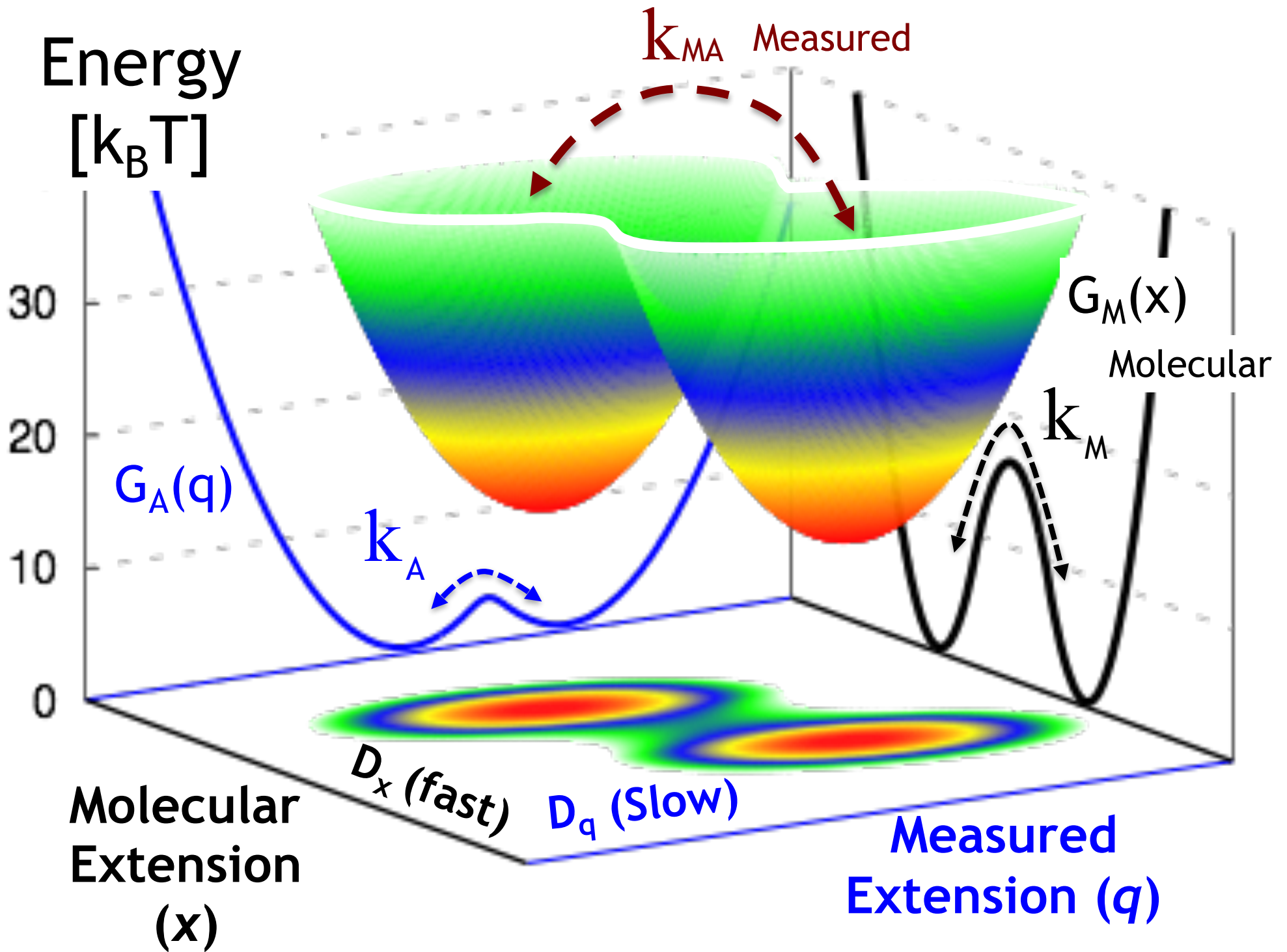


# Output from the experiment:



The molecular rate  $k_M$  is hidden.

The simplest picture that captures the essential physics: **anisotropic 2D diffusion** over the measured extension and the hidden molecular extension.



# Single-molecule

- Using **Langer's Theory** and following ref <sup>1</sup>, in the limit of high anisotropic diffusion (**very slow apparatus**)<sup>2</sup>:

$$\frac{1}{k_{MA}} \approx \frac{1}{k_M (1 - V''(q_U - x_U) / |G''_o(x_U)|)} + \frac{1}{k_A}$$

↓                      ↓                      ↓                      ↓                      ↓

Measured            Molecular            Linker stiffness            Molecular stiffness            Apparatus artifact

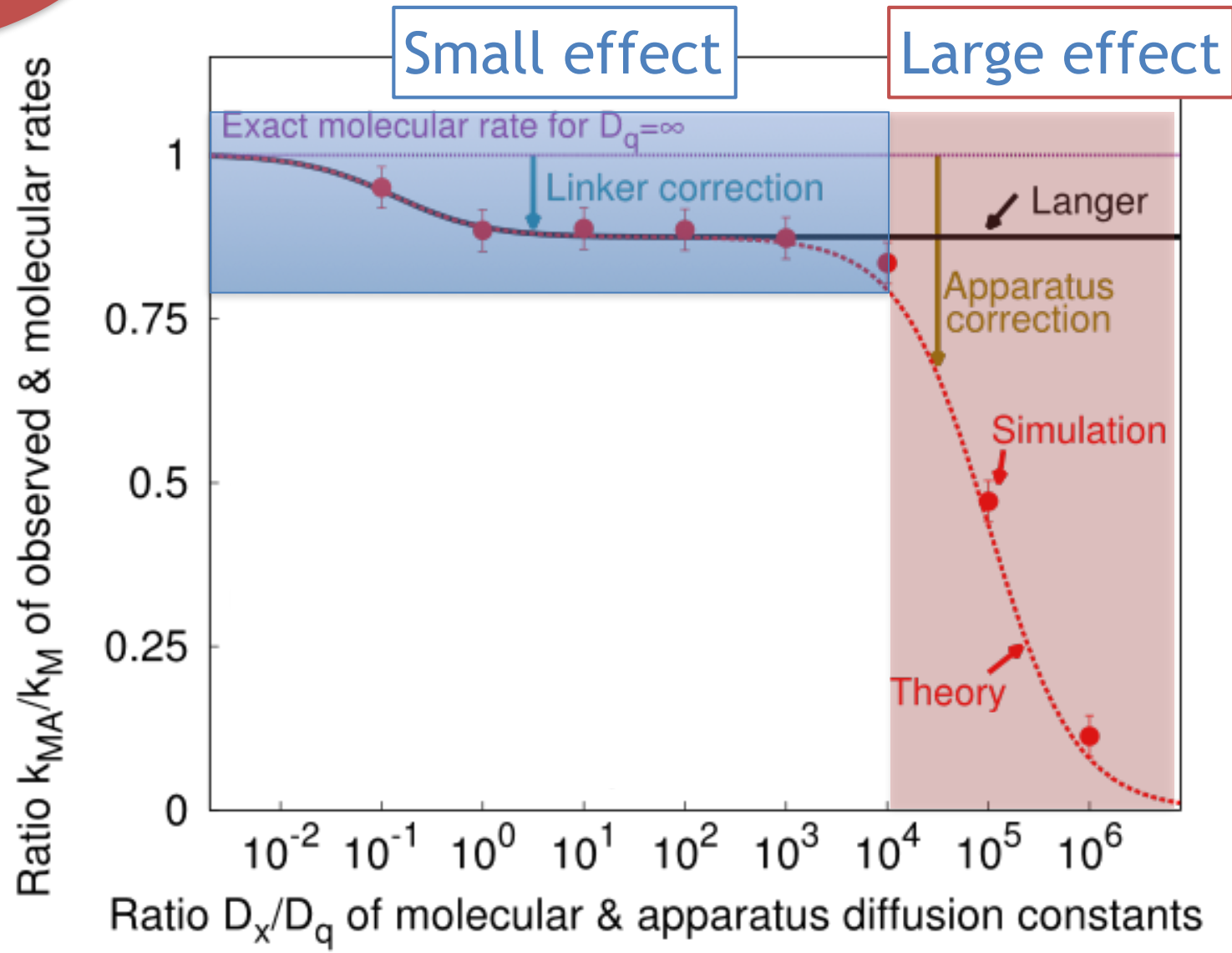
<sup>1</sup> Berezhkovskii AM, Szabo A, Greives N, Zhou HX. *J Chem Phys* (2014).

<sup>2</sup> **Cossio**, Hummer, Szabo. *Proc Natl Acad Sci U S A* (2015).

# Single-molecule

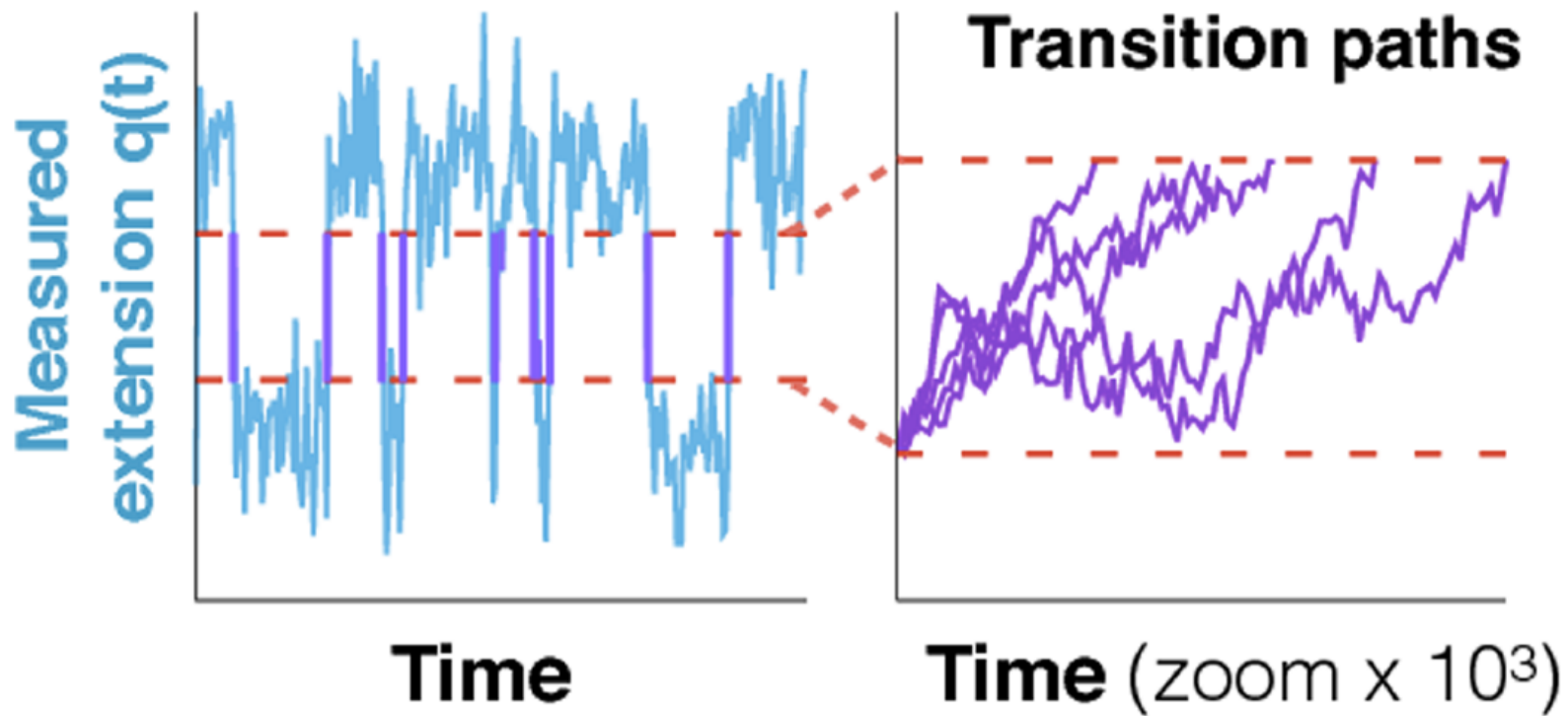
Use the analytical expressions to know in which regime the system is.

## Validation with 2D Brownian dynamics:



Single-  
molecule

What about the transition  
paths?



# Single-molecule

Recently it was possible to directly measure transition paths with force spectroscopy

## REPORT

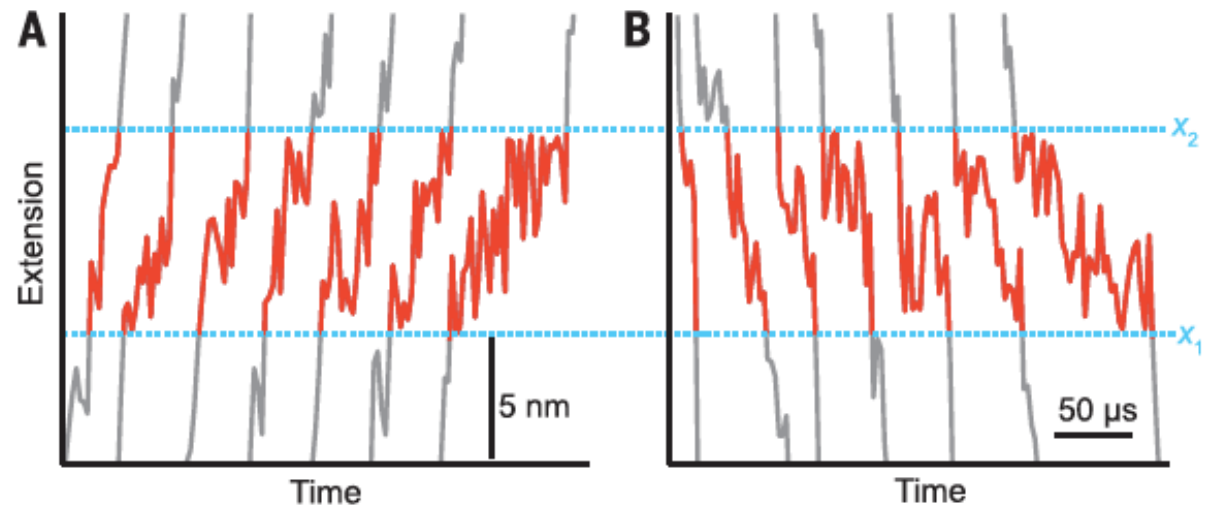
Direct observation of transition paths during the folding of proteins and nucleic acids

Krishna Neupane<sup>1</sup>, Daniel A. N. Foster<sup>1</sup>, Derek R. Dee<sup>1</sup>, Hao Yu<sup>1</sup>, Feng Wang<sup>2</sup>, Michael T. Woodside<sup>1,2,\*</sup>

\* See all authors and affiliations

Science 08 Apr 2016;  
Vol. 352, Issue 6282, pp. 239-242  
DOI: 10.1126/science.aad0637

**Fig. 2. Transition paths for a DNA hairpin.** Selection of transition paths for (A) unfolding and (B) refolding. Boundaries  $x_1$  and  $x_2$  (cyan) demark the barrier region. Transition paths display a wide variety of shapes and transit times.





# Single-molecule

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## REPORT

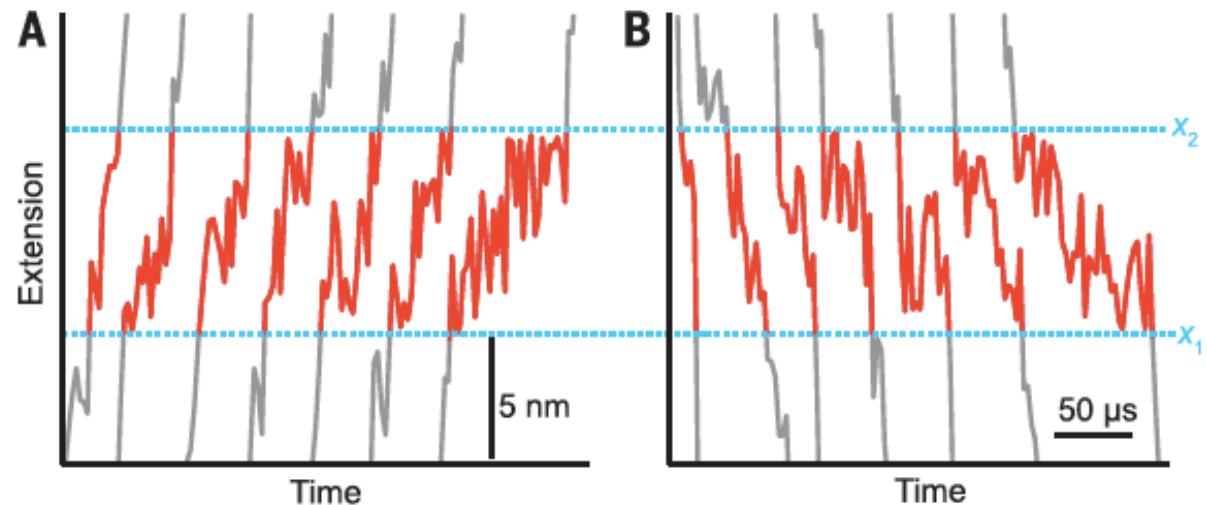
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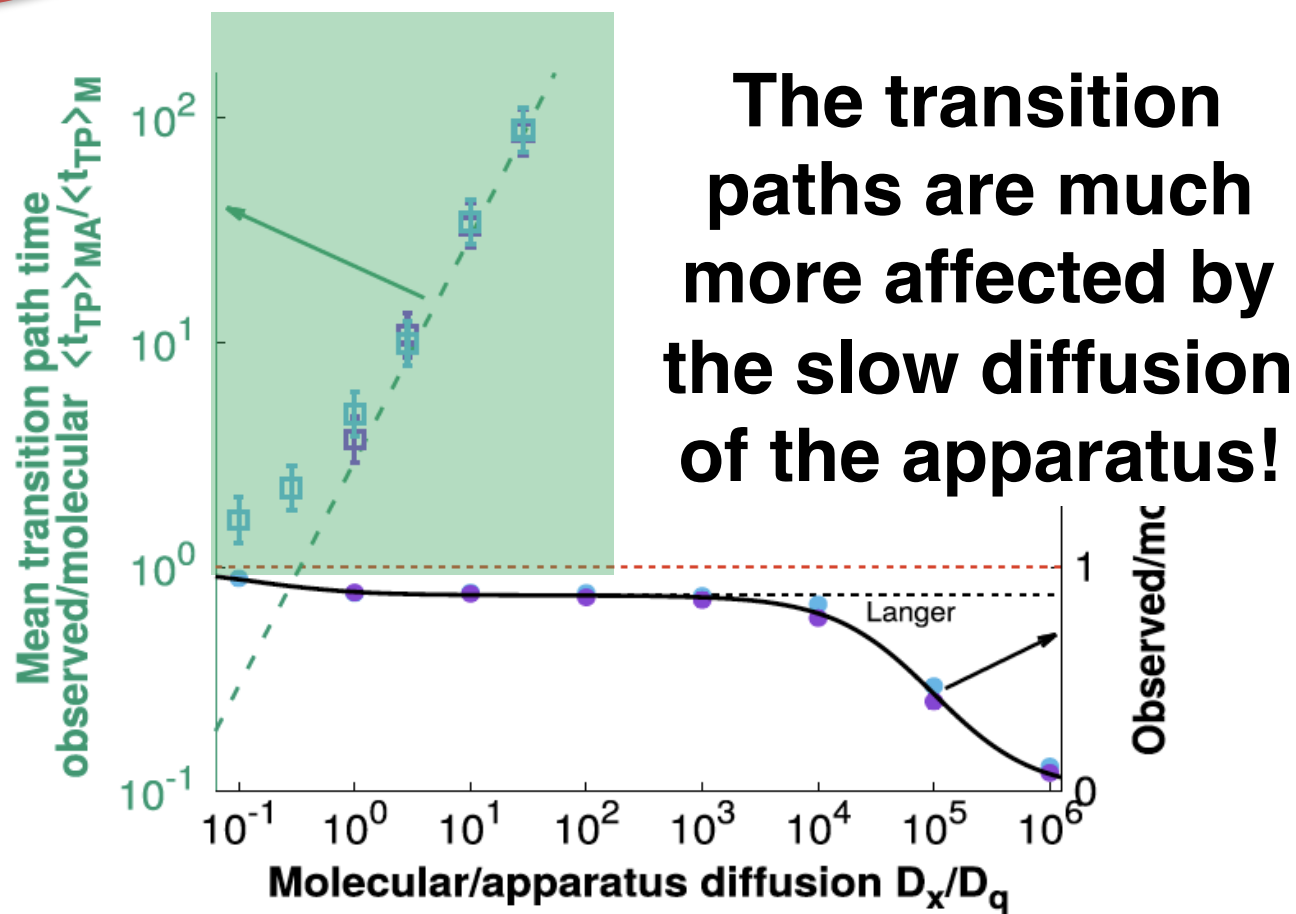
**Fig. 2. Transition paths for a DNA hairpin.** Selection of transition paths for (A) unfolding and (B) refolding. Boundaries  $x_1$  and  $x_2$  (cyan) demark the barrier region. Transition paths display a wide variety of shapes and transit times.



The authors claimed that the transition path time depends only on the **molecule**.

# Single-molecule

## Artifacts of the apparatus:



Our theory provides accurate analytic expressions to:

- extract information of the intrinsic free energy and dynamics of the molecule
- assess the effects of the pulling device on the unfolding transition rate and paths.

# Acknowledgements

My group:



**Prof.  
Hummer**



**Dr. Szabo**

**MAX PLANCK**  
GESELLSCHAFT



**ruta**<sup>n</sup>  
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CENTRO DE INNOVACIÓN Y NEGOCIOS



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